
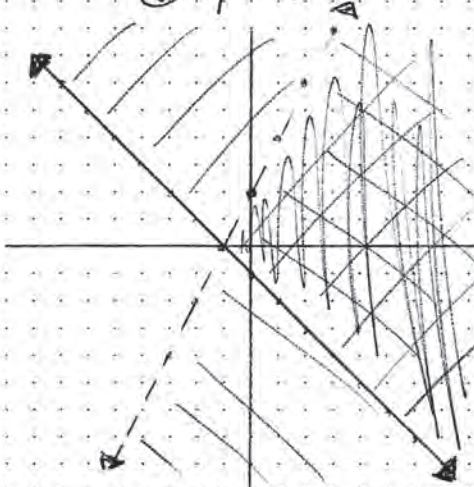
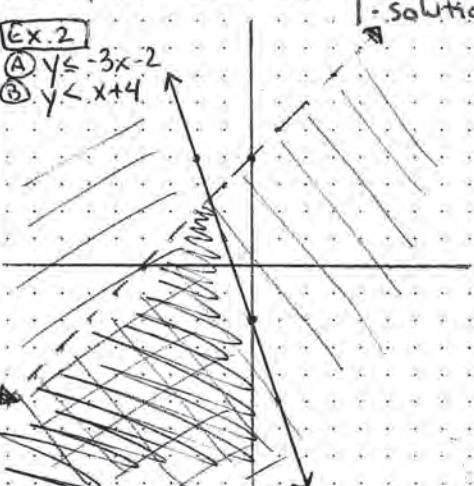


## TEACHER REFERENCE 8.3

CORNELL NOTES		TOPIC/OBJECTIVE:	NAME:																		
	<div style="font-size: 1.2em; margin-bottom: 10px;">Graphing</div> <div style="font-size: 1.2em;">system of linear inequalities</div>		<div style="font-size: 1.2em; margin-bottom: 10px;">Student Sample</div> <div style="font-size: 1.2em;">CLASS/PERIOD: Alg 1 / per. 3</div> <div style="font-size: 1.2em;">DATE: 3/12</div>																		
<b>ESSENTIAL QUESTION:</b> What similarities & differences exist between solving systems of linear equations & systems of inequalities?																					
<b>QUESTIONS:</b>  <div style="font-size: 1.1em;">How does solving</div> <div style="font-size: 1.1em;"><math>y &lt; 2x + 2</math></div> <div style="font-size: 1.1em;"><math>y \geq -x - 1</math></div> <div style="font-size: 1.1em;">compare/contrast with solving</div> <div style="font-size: 1.1em;"><math>y = 2x + 2</math></div> <div style="font-size: 1.1em;"><math>y = -x - 1</math>?</div>	<div style="border: 1px solid black; padding: 5px; margin-bottom: 10px;"> <b>Ex. 1</b>    ① <math>y &lt; 2x + 2</math>                         ② <math>y \geq -x - 1</math> </div>  <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>① Graph the 2 lines * remember to dot <math>&gt;</math> or <math>&lt;</math></p> <p>② Test points in equations * (0,0) easy to test</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; text-align: center;">(0,0)</td> <td style="width: 50%; text-align: center;">(0,0)</td> </tr> <tr> <td style="text-align: center;">① <math>y &lt; 2x + 2</math></td> <td style="text-align: center;">② <math>y \geq -x - 1</math></td> </tr> <tr> <td style="text-align: center;"><math>0 &lt; 2(0) + 2</math></td> <td style="text-align: center;"><math>0 \geq -0 - 1</math></td> </tr> <tr> <td style="text-align: center;"><math>0 &lt; 2</math></td> <td style="text-align: center;"><math>0 \geq -1</math></td> </tr> <tr> <td style="text-align: center;">True</td> <td style="text-align: center;">True</td> </tr> </table> <p>③ shade true areas</p> <p>④ Darkly shade overlap</p> </div> <div style="width: 50%; border-left: 1px solid black; padding-left: 10px;"> <div style="display: flex; justify-content: space-between; font-size: 0.9em;"> <span>same</span> <span>Diff</span> </div> <ul style="list-style-type: none"> <li>• Graph the same</li> <li>• inequalities have shaded regions of solutions</li> <li>• Solutions may not be on the line</li> </ul> </div> </div> <div style="border: 1px solid black; padding: 5px; margin-top: 10px;"> <b>Ex. 2</b>    ① <math>y \leq -3x - 2</math>                         ② <math>y &lt; x + 4</math> </div>  <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>① Graph the 2 lines</p> <p>② Test 2 points in equations</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; text-align: center;">(0,0)</td> <td style="width: 50%; text-align: center;">(0,0)</td> </tr> <tr> <td style="text-align: center;">① <math>0 \leq -3(0) - 2</math></td> <td style="text-align: center;">② <math>0 &lt; 0 + 4</math></td> </tr> <tr> <td style="text-align: center;"><math>0 \leq -2</math></td> <td style="text-align: center;"><math>0 &lt; 4</math></td> </tr> <tr> <td style="text-align: center;">False</td> <td style="text-align: center;">True</td> </tr> </table> <p>③ If false shade opposite area</p> <p>④ Darkly shade overlap</p> </div> </div>			(0,0)	(0,0)	① $y < 2x + 2$	② $y \geq -x - 1$	$0 < 2(0) + 2$	$0 \geq -0 - 1$	$0 < 2$	$0 \geq -1$	True	True	(0,0)	(0,0)	① $0 \leq -3(0) - 2$	② $0 < 0 + 4$	$0 \leq -2$	$0 < 4$	False	True
(0,0)	(0,0)																				
① $y < 2x + 2$	② $y \geq -x - 1$																				
$0 < 2(0) + 2$	$0 \geq -0 - 1$																				
$0 < 2$	$0 \geq -1$																				
True	True																				
(0,0)	(0,0)																				
① $0 \leq -3(0) - 2$	② $0 < 0 + 4$																				
$0 \leq -2$	$0 < 4$																				
False	True																				
<b>SUMMARY:</b>																					

QUESTIONS:

NOTES:

**Ex. 3**

①  $y < \frac{1}{3}x + 5$

②  $y \geq -2x$

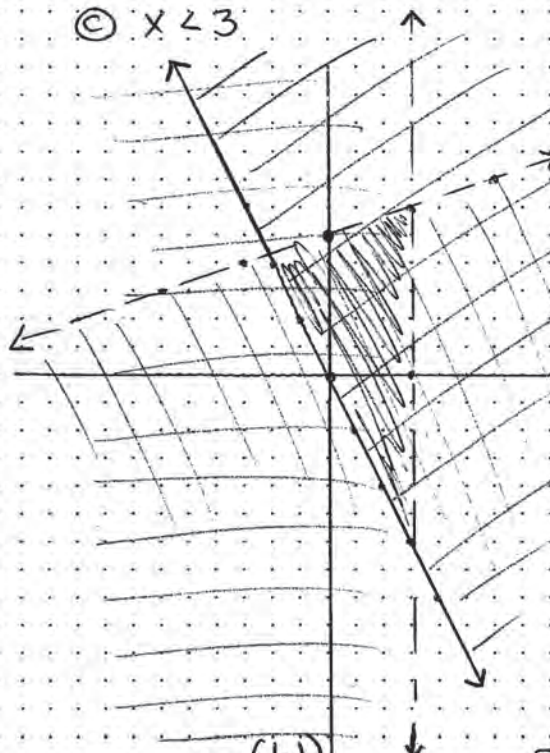
③  $x < 3$

Apply the  
process  
for graphing  
2 inequalities  
onto

$y < \frac{1}{3}x + 5$

$y \geq -2x$

$x < 3$



① Graph the 3 equations.

② Test points in each equation

\*if line passes through ~~another~~ (0,0) use another point

① (0,0)  
 $y < \frac{1}{3}x + 5$   
 $0 < \frac{1}{3}(0) + 5$   
 $0 < 5$

**True**

② (1,1)  
 $y \geq -2x$   
 $1 \geq -2(1)$   
 $1 \geq -2$

**True**

③ (0,0)  
 $0 < 3$

**True**

SUMMARY:

The basics of graphing inequalities are the same as graphing equations. You start at the y-intercept & use slope. Make sure to check if the line is dotted or solid. You also need to test a point to shade.





Solving multi-step  
equations

Student B

Algebra (Per. 5)

10/11

## ESSENTIAL QUESTION:

How can we combine our knowledge of  $x$ ,  $\div$ ,  $+$ ,  $-$  with our distributive & combining term skills to solve multiple step equations?

## QUESTIONS:

Apply the  
process for  
solving

$$9x - 4x - 6 = 19$$

onto

$$5p + 3(2p + 1) = 25$$

**Ex 1**

$$9x - 4x - 6 = 19$$

$$\begin{array}{r} 5x - 6 = 19 \\ +6 \quad +6 \end{array}$$

$$\begin{array}{r} 5x = 25 \\ \underline{5} \quad \underline{5} \\ x = 5 \end{array}$$

① Combine terms

② Isolate  $x$  by adding

③ Divide by coefficient

④ Check your answer

check  
 $9(5) - 4(5) - 6 = 19$

$$45 - 20 - 6 = 19$$

$$25 - 6 = 19$$

$$19 \neq 19$$

$5p + 3(2p + 1) = 25$  would 1<sup>st</sup> require you to distribute.  
Also we would need to isolate  $x$  by subtracting  
since it is  $5p + 6p + 3 = 25$

**Ex. 2**

$$5p + 3(2p + 1) = 25$$

$$5p + 6p + 3 = 25$$

$$\begin{array}{r} 11p + 3 = 25 \\ -3 \quad -3 \end{array}$$

$$\begin{array}{r} 11p = 22 \\ \underline{11} \quad \underline{11} \\ p = 2 \end{array}$$

① Distribute

② Combine terms

③ Isolate variable  
by  $+$ / $-$

④  $\div$  by coefficient  
⑤ check answer

check  
 $5(2) + 3(2(2) + 1) = 25$

$$10 + 3(4 + 1) = 25$$

$$10 + 3(5) = 25$$

$$10 + 15 = 25$$

$$25 \neq 25$$

**Ex. 3**

$$2(2m + 4) - (2m - 3) = 17$$

$$4m + 8 - 2m + 3 = 17$$

$$2m + 11 = 17$$

$$\begin{array}{r} 2m + 11 = 17 \\ -11 \quad -11 \\ \hline 2m = 6 \\ \hline \frac{2m}{2} = \frac{6}{2} \end{array}$$

$$m = 3$$

① Distribute ( $\times 2$ )

② combine terms

③ Isolate variables  
by  $+$ / $-$

④  $\div$  by coeff.

⑤ check answer

check

$$2(2(3) + 4) - (2(3) - 3) = 17$$

$$2(6 + 4) - (6 - 3) = 17$$

$$2(10) - (3) = 17$$

$$20 - 3 = 17$$

$$17 \neq 17$$

## SUMMARY:

Having parenthesis in an equation will require you to distribute as the first step. After that the combining terms, isolating variables, and dividing by coefficients are the same. Although need to be careful about isolating by  $+$  or  $-$ .

# Solving Systems of Equations (SoE)

## Essential Question:

How do you solve (SoE) by substitution?

→ solution will be an ordered pair like (3, 2)

## Questions:

What is a system of linear eq.?

What are the steps to solving SoE by sub.?

## Notes

System of linear equations (SoE) - 2 or more linear equations in the same variables.

Steps to solving by sub.: *if possible,*

1. Solve 1 eq for its variable. *Solve for variable w/ coeff. of 1 or -1.*
2. Sub the expression from Step 1 into other eq.
3. Solve that eq. to get value of 1<sup>st</sup> var.
4. Sub value of 1<sup>st</sup> var. into original eq. & solve for 2<sup>nd</sup> var.
5. Write the values from #3 & #4 as an ordered pair.
6. Check?

Ex. Solve

$$y = 3x + 2$$

$$x + 2y = 11$$

(Eq. #1)

(Eq. #2)

Step 1

$$y = 3x + 2$$

$$x + 2y = 11$$

← Eq. 1 already solved for y.

## Summary:



## Questions:

Now do ↓

Apply the steps  
of solving (SoE)  
to the (SoE)

$$y = 3x + 2$$

$$x + 2y = 11$$

## Notes:

Step 2

$$y = 3x + 2$$

$$x + 2y = 11$$

$$x + 2(3x + 2) = 11$$

Step 3

$$x + 6x + 4 = 11$$

$$7x + 4 = 11$$

$$\begin{array}{r} -4 \quad -4 \\ \hline \end{array}$$

$$7x = 7$$

$$\begin{array}{r} \overline{7} \quad \overline{7} \end{array}$$

$$(x = 1)$$

Step 4

$$y = 3x + 2$$

$$y = 3(1) + 2$$

$$y = 3 + 2$$

$$(y = 5)$$

Step 5

$$(1, 5)$$

\* Check : ?

Eq. 1

$$y = 3x + 2$$

$$5 = 3(1) + 2$$

$$5 = 3 + 2$$

$$5 = 5 \checkmark$$

Sub.  $3x + 2$  for  $y$  in 2nd eq.

Simplify (Use Dist.)  
(Collect terms)

Subtract 4 from  
both sides

÷ by 7 > to isolate  
the variable

Write 1st eq.

Sub. 1 for  $x$

Simplify for  $y$

Write SoE as ordered pair

on my test,  
do I need to  
check my  
answers in  
both  
equations?  
or just  
one?

Eq. 2

$$x + 2y = 11$$

$$1 + 2(5) = 11$$

$$1 + 10 = 11$$

$$11 = 11 \checkmark$$

## Summary:

### Questions:

Now do I apply  
the process  
for solving

$$y = 3x + 2$$

$$x + 2y = 11$$

to the (SoE)

$$y = 2x + 1$$

$$2y - x = 11?$$

### Notes:

Step 1

$$y = 2x + 1$$

$$2y - x = 11$$

Step 2

$$2(2x + 1) - x = 11$$

Step 3

$$4x + 2 - x = 11$$

$$3x + 2 = 11$$

$$\begin{array}{r} -2 \quad -2 \\ \hline \end{array}$$

$$\begin{array}{r} 3x = 9 \\ \hline 3 \quad 3 \end{array}$$

$$\boxed{x = 3}$$

Step 4

$$y = 2(3) + 1$$

$$y = 6 + 1$$

$$\boxed{y = 7}$$

Step 5

$(3, 7)$ -ordered pair

Step 5  
Check:

Eq. 1

$$7 = 2x + 1$$

$$7 = 2(3) + 1$$

$$7 = 6 + 1$$

$$7 = 7 \checkmark$$

Eq. 2

$$2y - x = 11$$

$$2(7) - 3 = 11$$

$$14 - 3 = 11$$

$$11 = 11 \checkmark$$

(Same process for both SoE)

How is solving  
SoE using sub.  
diff. than  
graphing?

• Graphing not good for getting an exact intersection point.

• Substitution - get an ordered pair.

### Summary:

A system of linear equations is two or more linear equations with the same variables. The sub. method has you isolate one variable in an equation and plug it into the other equation. Following these five steps and checking my answer will ensure the my ordered pair is the correct solution.



# Graphing Trig Functions

How can I successfully graph all six trigonometric functions?

Determine how to graph the function if there is a phase shift?

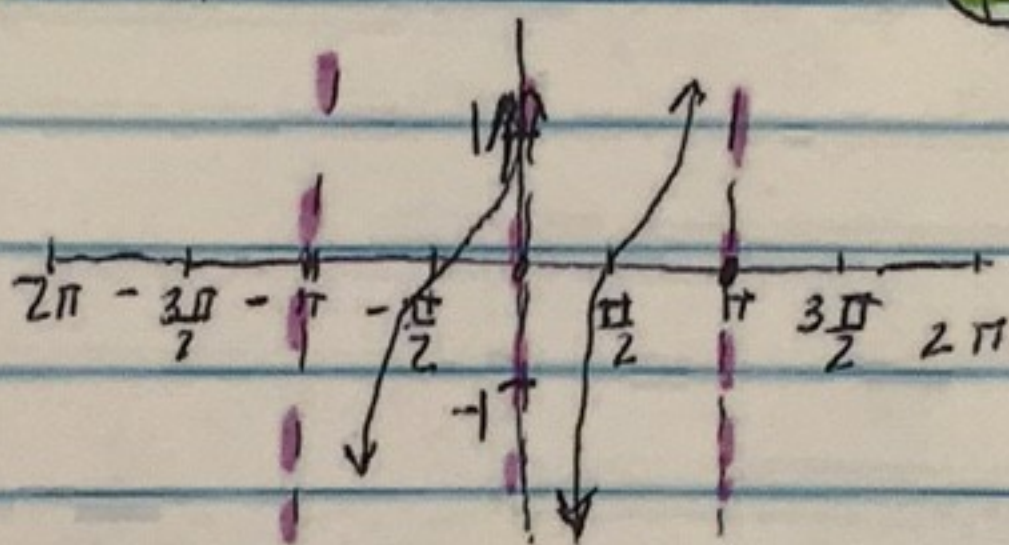
Graph:  $y = \tan(x + \pi/2)$

$A = 1$

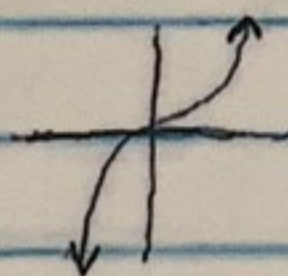
$P = |\frac{\pi}{b}| = \pi$

$C = -\pi/2 \leftarrow$

\*phase shift moves left or right (depending on sign)



Parent function of tangent



Which formula can I use to

$x$ -intercepts  $= \pi n$

Identify the vertical asymptotes?

Vertical asymptotes  $= x = \frac{\pi}{2} + \pi n$

\*represents integer

Original form of tangent

$y = a \tan(bx - c) + d$

Determine how to find the key points in graphing for tangent?

\*amplitude

used to find  
\*period  
 $(\frac{\pi}{|b|})$

\*phase shift

\*vertical shift  
(moves up or down)

In order to graph a trigonometric function we need to determine if there are phase shifts or vertical shift. If so, we need to identify them correctly and plot them on the graph. The vertical asymptotes are used to show where the graph is undefined and draw a dotted line,  $n$  represents an integer.





## Systems of equations

Algebra 2

March 26, 2015

ESSENTIAL QUESTION:

How can I solve systems of equations?

QUESTIONS:

NOTES:

What is systems of equations?

**Systems of Equations** – A set or collection of

equations that you deal with all together at once. Linear equations (ones that graph as straight lines) are simpler than non-linear equations, and the simplest linear system is one with two equations and two variables.

What are 2 ways to solve it?

- ★ 1. Substitution  $3x + 2y = 12$  with  $y = x - 9$   
 2. Elimination  $4x + 5y = 16$  subtracts  $4x + 10y = 160$

Show the steps of solving one?

1. Determine if you choose to use substitution or elimination  $2x + 4y = -2$   
 $Y = (x + 8)$

Include numbers

2. Plug in Y  $2x + 4(x - 8) = -2$   
 3. Distribute  $2x + 4x - 32 = -2$   
 4. Combine like terms  $6x - 32 = -2$   
 5. Get X on one side  $6x = 30$   
 6. Divide  $6/6x = 30/6$   
 7. Get X  $X = 5$   
 8. Plug X in to find Y and solve  $2(5) + 4y = -2$

SUMMARY:

Systems of equations give 2 equations for us to solve it.

There's 2 ways to do it; substitution and elimination. Both will give the same answer. When you know Y, plug it in and use substitution. You can multiply an equation and subtract it from the other, using elimination.





Raising a power to a power

Algebra 2

3/27/15

ESSENTIAL QUESTION:

How can you raise a power to a power in Math?

QUESTIONS:

NOTES:

What are the rules?

- Rule 1 :  $(x^m)^n = x^{(m)(n)}$ - Rule 2 :  $(xy)^m = x^m y^m$ 

What is a Polynomial?

Polynomial - An expression with many terms

outside of the parenthesis

What are the steps?

1. Distribute the exponent
2. Multiply the bases (Coefficients)
3. Write down the correct form

How can you tell if you need to raise a power to a power?

To tell if a problem requires you to raise a power to a power, look for the exponent OUTSIDE of the parenthesis. If it has an exponent, distribute it

Example problems and solve them?

8.  $(5xy^2)(4x^3y^3)$

$[20x^4y^5]$

9.  $-(9x^2y^4)^2(x^3)^4$

$-(9^2(x^2)^2(y^4)^2)(x^{12})$   
 $-(81x^4y^8)(x^{12}) = [-81x^{16}y^8]$

11.  $(-6d^2+d) - (d^2+d)$

$-6d^2+d-d^2-d$   
 $[-7d^2]$

12.  $3xy^9 - 7x(y^3)^3$

$3xy^9 - 7xy^9 = [-4xy^9]$

14.  $-5(2x^3d)^2(x^4d)^5$

$-5(2^2(x^3)^2d^2)(x^4)^5d^5$   
 $-5(4x^6d^2)(x^{20}d^5)$   
 $[-20x^{26}d^7]$

15.  $7a^2(3ab^3)(4b)^2$


$7a^2(3ab^3)(16b^2)$   
 $[336a^3b^5]$

SUMMARY:

The rules of raising a power to a power in Math are :

$(x^m)^n = x^{(m)(n)}$ , and  $(xy)^m = x^m y^m$ . Polynomials are involved.

Fractions and decimals may also have an appearance. The bases are the coefficients. To raise a power to a power, an exponent is needed outside.

<b>CORNELL NOTES</b> 	TOPIC/OBJECTIVE:	NAME: <span style="border: 1px solid black; display: inline-block; width: 150px; height: 25px; vertical-align: middle;"></span>
	Factoring Polynomials	CLASS/PERIOD: Algebra 1
		DATE: 2015 March 23

ESSENTIAL QUESTION: Using your math skills, how would you factor polynomials ?

QUESTIONS:	NOTES:
What is factoring ?	★ <span style="border: 1px solid red; padding: 2px;">Factoring</span> - The process of separating a polynomial back into a product
Using math terms you use in class, give the definition of a polynomial ?	<span style="border: 1px solid red; padding: 2px;">Polynomial</span> - An expression of more than two Algebraic terms, especially the sum of several terms that contain different powers of the same variables  Polynomials that cannot be factored are called Prime
What's GCF ?	<span style="border: 1px solid red; padding: 2px;">GCF</span> - Greatest common factor
Identify the steps taken to solving this problem ?	★ 1. Look at coefficients first 2. A variable must be common to all terms to be a GCF 3. If a variable is common to all terms, take the one with the smallest exponent 4. Divide all terms by the GCF to get remainder in parenthesis
Solve the following problems for practice	$3a^3b^2c - 9a^2b^3c^2 + 15ab^4c^3$  $15a^2b - 30ab$  $8m + 36n$

SUMMARY: When factoring polynomials, you must follow the math rules. Looking at the coefficients, what would be the GCF ? A variable is required to be common to all the terms to be a GCF. The smallest exponent will be used. After these steps, divide all terms by the GCF to get the remainder in parenthesis. These are the steps and process to factoring polynomials.





Integer

Algebra 2

March 25, 2015

ESSENTIAL QUESTION:

How can students successfully use models to ( x and / ) integers?

QUESTIONS:

NOTES:

Can you identify what is an integer?



Integer - Any number, regardless of its sign.

Includes positive and negative #'s

What type of number would be the outcome of a positive times a negative?

If you multiply a positive times a negative number, the result of the problem would be a negative

number  $P(N) = N$ 

$$\text{Ex : } 100(-5) = -500$$

$$2(-16) = -32$$

What type of number would be the outcome of a negative times a negative?

If you multiply a negative with a negative, the outcome of the problem would always be a positive

number  $N(N) = P$ 

$$\text{Ex : } -6(-13) = 78$$

$$-2(-16) = 32$$

Would the rule apply to others?



This rule is valid whenever you deal with multiplying or dividing negative numbers with positive or negative. Does not work with addition or subtraction

SUMMARY:

An Integer is any number, regardless of its sign. When adding and subtracting integers, you do not follow the rule. However, if you multiply and divide integers, you are required to use the rule.

A  $P(N) = N$  and a  $N(N) = P$ . Use this rule in equations too.



# Graphing systems Of equations

ESSENTIAL QUESTION: Using my knowledge of math, how can I determine the solution to a system of equations?

QUESTIONS:

Explain what it means to solve a system of equations?

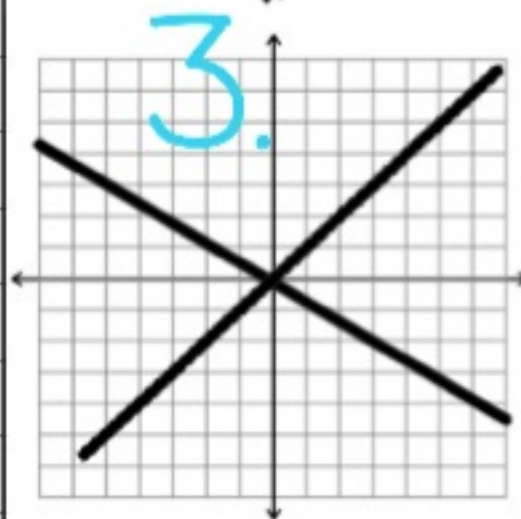
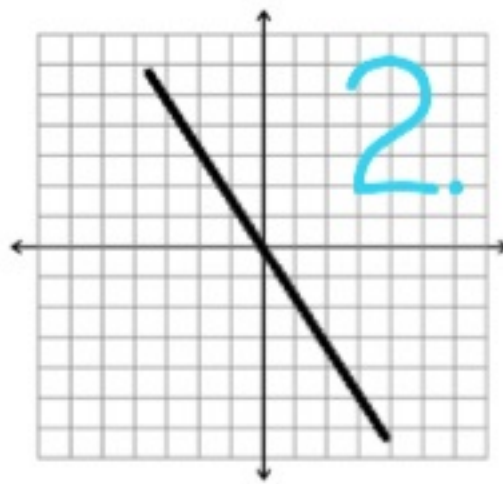
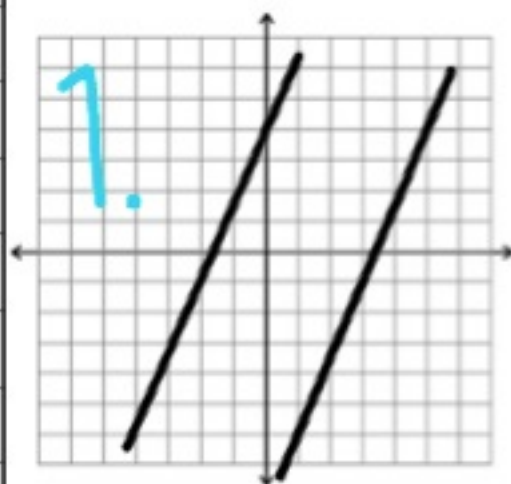
NOTES:



(X, Y)

Solution to a system is a point that makes both equations true. A point that intersects all lines  
Graph the equation. If none / infinite, don't find point.  
If one, find point.

Depict the diff. solutions of a Graph and explain how they differ from each other?



1. No solution.

They never meet at a point

2. Infinite solution.

They are the same

3. One solution.

There is a point where they meet

Solutions



-Study for quiz 1.29.15

SUMMARY:

To solve a set of equations, you determine the point that makes the Solutions both true. First, you graph the slope-Intercept form onto the graph. Second, you determine if they cross each other. Then, you solve if both equations equal each other, to get X. Next, you plug in X to find Y, and you get your point.